

A Matematika Tudáselméleti- és Pszichológiai Kutatócsoport Umeåban





PME42
42nd Annual Meeting
July 3-8, 2018
Umeå, Sweden

PME = Psychology of Mathematics Education

„Minden”, ami a matematikai gondolkodás témakörébe tartozik.

1. Mi az a „minden”?
2. Mi az, ami a „mindenen” kívül van?



PM

„Minden”

1. Mi az a

2. Mi az, a

rtozik.

Egy nap a konferencián



- PL= Plenary Lecture
- RR = Research Reports
- OC = Oral Communications



Egy nap a konferencián

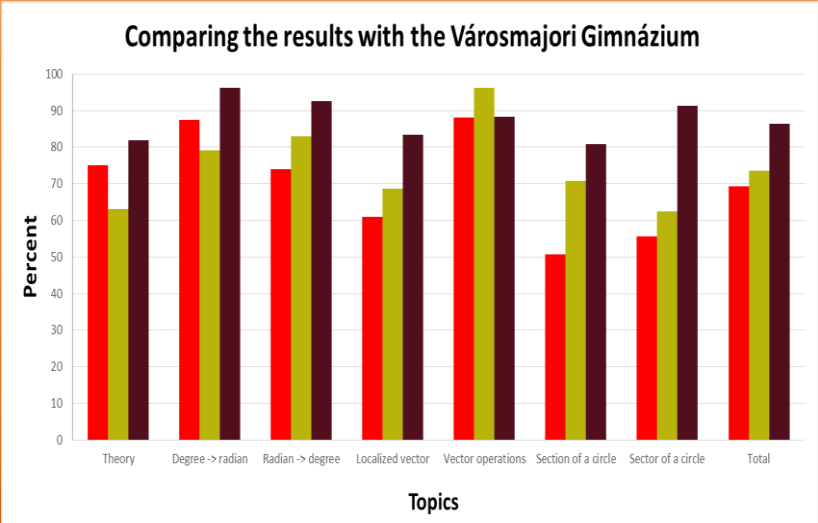
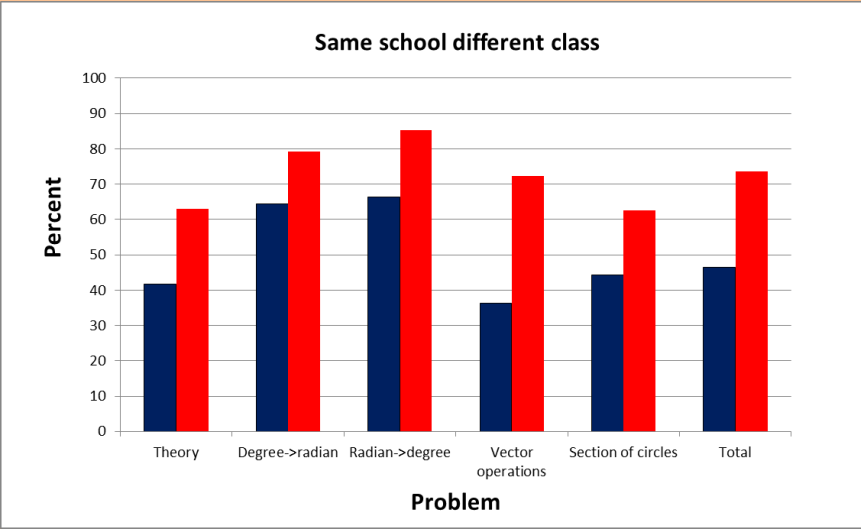


- CO = Colloquium
- WG= Working Group
- PP=Poster Presentation



9:00am - 10:30am	Plenary Lecture 2: Nathalie Sinclair - "AN AESTHETIC TURN IN MATHEMATICS EDUCATION" Location: Aula Nordica										+					
11:00am - 11:40am	RR 1:01 Location: N410	+	RR 1:02 Location: N420	+	RR 1:03 Location: N430	+	RR 1:04 Location: N440	+	RR 1:05 Location: N450	+	RR 1:06 Location: N460	+	RR 1:07 Location: N300 Cancelled!	+	RR 1:08 Location: N320	+
	RR 1:09 Location: N330	+	RR 1:10 Location: N360 New chair!	+	RR 1:11 Location: N370	+	RR 1:12 Location: N380	+	RR 1:13 Location: N210	+	RR 1:14 Location: N230	+	RR 1:15 Location: N260	+	RR 1:16 Location: N270	+
	RR 1:17 Location: MC313	+	RR 1:18 Location: MC333	+	RR 1:19 Location: MC343	+	RR 1:20 Location: MA346	+								
11:50am - 12:30pm	RR 2:01 Location: N410	+	RR 2:02 Location: N420	+	RR 2:03 Location: N430	+	RR 2:04 Location: N440	+	RR 2:05 Location: N450	+	RR 2:06 Location: N460	+	RR 2:07 Location: N300 New chair!	+	RR 2:08 Location: N320	+
	RR 2:09 Location: N330	+	RR 2:10 Location: N360	+	RR 2:11 Location: N370	+	RR 2:12 Location: N380	+	RR 2:13 Location: N210	+	RR 2:14 Location: N230	+	RR 2:15 Location: N260	+	RR 2:16 Location: N270	+
	RR 2:17 Location: MC313	+	RR 2:18 Location: MC333	+	RR 2:19 Location: MC343	+	RR 2:20 Location: MA346	+								
2:00pm - 3:00pm	OC 1:01 Location: N410 Topic: Mathematics difficulties	+	OC 1:02 Location: N420 Topic: ICT and learning, Grade 7-9	+	OC 1:03 Location: N430 Topic: Classroom assessment	+	OC 1:04 Location: N440 Topic: Geometry, space and shape	+	OC 1:05 Location: N450 Topic: Preservice teachers, Practice experience	+	OC 1:06 Location: N460 Topic: Tasks in algebra and functions One presentation was cancelled!	+	OC 1:07 Location: N300 Topic: Proof, argumentation and reasoning	+	OC 1:08 Location: N330 Topic: Representations and modeling	+
	OC 1:09 Location: N370 Topic: Professional development programs	+	OC 1:10 Location: N380 Topic: Probability and statistics	+	OC 1:11 Location: N210 Topic: Preservice teachers and teaching	+	OC 1:12 Location: N230 Topic: Arithmetic, numbers and operations	+	OC 1:13 Location: N260 Topic: ICT, GeoGebra in Higher education	+	OC 1:14 Location: N270 Topic: Proportions	+	OC 1:15 Location: MC333 Topic: Affect, emotions and attitudes	+	OC 1:16 Location: MC343 Topic: Affect, emotions and attitudes	+
	OC 1:17 Location: MA346 Topic: Problem solving, Grade 8	+														
3:10pm - 3:50pm	RR 3:01 Location: N410	+	RR 3:02 Location: N420	+	RR 3:03 Location: N430	+	RR 3:04 Location: N440	+	RR 3:05 Location: N450	+	RR 3:06 Location: N460	+	RR 3:07 Location: N300	+	RR 3:08 Location: N320	+
	RR 3:09 Location: N330	+	RR 3:10 Location: N360	+	RR 3:11 Location: N370	+	RR 3:12 Location: N380	+	RR 3:13 Location: N210	+	RR 3:14 Location: N230	+	RR 3:15 Location: N260	+	RR 3:16 Location: N270	+
	RR 3:17 Location: MC313	+	RR 3:18 Location: MC333	+	RR 3:19 Location: MC343	+	RR 3:20 Location: MA346	+								
4:30pm - 6:00pm	WG 01 part 1 Location: N410	+	WG 02 part 1 Location: N260	+	WG 03 part 1 Location: N270	+	WG 04 part 1 Location: MC313	+	WG 05 part 1 Location: N420	+	WG 06 part 1 Location: N430	+	WG 07 part 1 Location: MA346	+	WG 08 part 1 Location: N440	+
	WG 09 part 1 Location: MA356	+	WG 10 part 1 Location: MA336	+	WG 11 part 1 Location: MA446	+	WG 12 part 1 Location: MA456	+	WG 13 part 1 Location: MA466	+	WG 14 part 1 Location: N450	+	WG 15 part 1 Location: MA476	+		

Research Report



Poster Section



- 2 poszter:

1. Előhívási hatás

– középiskolai kísérlet

2. Beöltöztetett feladatok





DRESSED UP PROBLEMS – THE DANGER OF PICKING THE INAPPROPRIATE DRESS

Eötvös Loránd University, Department of Algebra and Number Theory, SZEIBERT Janka, MUZSNAY Anna, SZABÓ Csaba, ZÁMBÓ Csilla

e-mail: szeibert.janka@gmail.com



42nd Annual Meeting of the International Group for the Psychology of Mathematics Education

PROBLEM 1.: There are four oil wells, so-called rockers, on an oil field. The oil is conducted from the rockers to the oil storage facility by a transmission pipeline. Where should the storage facility be built in order to minimize the length of pipelines? (The rockers are located at the vertices of a convex quadrilateral: ABCD.) /Matematika 9. OFI/

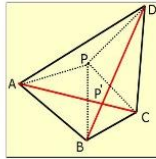
1995	1996	1997
204	288	339

PROBLEM 2.: The table contains data from three different years on the number of deaths caused by drugs in Hungary. Give a prediction for the year 2010. /Matematika 11. Mozaik/

PROBLEM 3.: How many different passwords can be made if you are only allowed to use the letters of the English alphabet a.) and a password is 6 characters long and all letters has to be distinct? b.) and a password is 6 characters long and repetition of characters is permitted? /Matematika 11. OFI/



PROBLEM 3. question c.): What can be question c.) if we know that the sample solutions of the book are wrong for a.) and b.)?



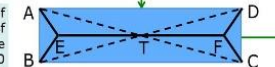
ANSWER ACCORDING TO THE TEACHERS' HANDBOOK: At the intersection of the diagonals. Sketch of the proof: let P be an internal point of the quadrangle, which is not located on the diagonals. According to the triangle inequality $PA+PC > AC$, $PB+PD > BD$, which means the total distance from the four vertices of the ABCD convex square to the point is longer than the distance of the two diagonals.

The abovementioned problems all have the property that while reading them, one can already be sure that the books' sample solutions are wrong.

REMARKS: 1. Since the flows, once the pipeline configuration is fixed, the storage facility can be located anywhere along the pipeline system. Hence, the answer cannot be correct.



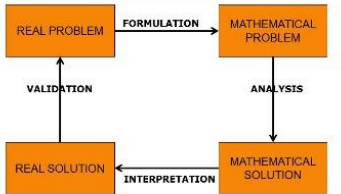
2. It is not even true that the sum of the diagonals minimizes the length of the system. In case of a rectangle if the diagonals have an angle less than 60 degrees, replacing one of the diagonals with two appropriate sides, a shorter path is obtained.



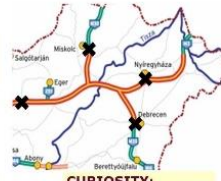
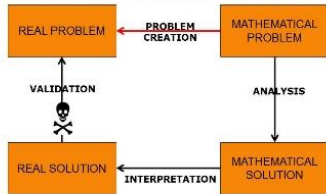
4. The solution of the problem in the generic situation is given by one of the Steiner trees of the points ABCD.



MODELLING CYCLE



THE PROCESS OF DRESSING UP



CURIOSITY: One of the applications of Steiner trees is the highway construction. Nyíregyháza, Debrecen, Miskolc, Budapest, are Hungarian cities.

In modeling, we solve a problem that is mostly outside mathematics by placing it in a mathematical context. (Greifrath, 2007)

Dressing means, the designation of a task around a given mathematical content in a way that the task seems to have real content. The main purpose is to create an impression of modeling problem or a problem which is close to reality.

REMARKS:

In case of problem 2. it can be noticed easily that a correct prediction can not be given based on only three data.

The question c.) of problem 3. is the following: How does the answer to question a.) and b.) changes, if you are allowed to use the lower case and capital letters, as well? Answer: It does not change at all.

CURIOSITY:

According to the textbook's solution, 35980 or 9202 people "will" lose their lives in 2010 caused by drugs. In fact this number was 17 in 2010.

CONCLUSION:

These problems are all dressed up problems, where the mathematical idea was born sooner than the real problem. The problem creator is not necessarily able to validate, verify his/her own problem. A possible way to avoid these errors in validation is a more thorough, professional refereeing of the context problems.



Efficiency of test-enhanced learning in teaching elementary geometry

Eötvös Loránd University Faculty of Science, Department of Algebra and Number Theory, 1117 Budapest, Pázmány Péter sétány 1/C Csilla Gyöngyvér ZÁMBÓ, Anna MUZSNAY, Janka SZEIBERT, Csaba SZABÓ e-mail: csilla95@gmail.com, csaba@cs.elte.hu, annamuzsnay@gmail.com, szeibert.janka@gmail.com



42nd Annual Meeting of the International Group for the Psychology of Mathematics Education

Motivation

In a recent review of studies on the intrinsic effect of testing, Roediger and Karpicke provided evidence that testing students on studied material results in improved retention of that material compared with spending an equivalent amount of time restudying the material. In their experiment, students studied prose passages and took three immediate free-recall tests, without feedback, or restudied the material the same number of times as the students who received tests. Students then took a final retention test 5 min, 2 days, or 1 week later.

	3x read	1x read, 2x tested
5 min later	80%	75%
2 days later	55%	70%
1 week later	40%	55%

Question: what is the effect of retrieval learning in mathematics classes in high school compared to a) pupils with the same skills and b) elite highschool students of high abilities.

Before:	Now:
• Laboratory	• Real life
• Psychology students	• Grade 9 pupils (highschool)
• Text/foreign words memorizing	• Mathematics lessons

Our hypotheses: retrieval effect already has its benefits at grade 9: students who study in a retrieval-enhanced way will perform better in comparison with previous results of themselves and other 9th graders of the same school and will perform similarly to students of an elite secondary school, who learn on the standard way.

Our Experiment is a real life experiment.

Topics - Elementary geometry:

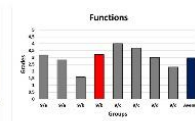
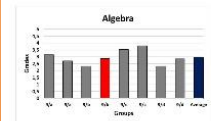
Arcs, sections of circles, arclength
Geometric transformations
Symmetric quadrangles
Regular polygons
Vectors

Test at the end of each lesson:

- From the material learnt the same day
- 2 questions: 1 theoretical, 1 practical
- Grading: 1 point each question
- The score counts in the final grade

In the original plan we wanted the pupils to submit the solution of a geometry problem to the teacher by email on the weekends, before Sunday evening. Most pupils did it on the first week. From the second week almost nobody did it. Several efforts of the teacher failed to have them to do the extra homework.

Control group from the same school

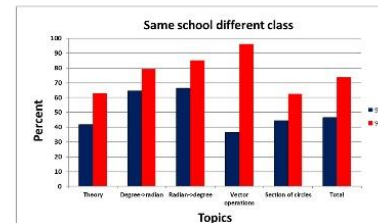


Control group from an elite school

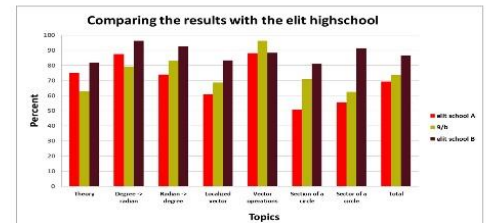
Experimental group	Control groups
• One group from 9 b.	• 9.c and 9.e classes (same teacher)
• 9 students	• 16, 18 students
• 3 lessons/week, 3-4 weeks	• 4 lessons/week, 4-5 weeks
• Total: 11 lessons	• Total: 19, 16 lessons
• Vocational school	• Grammar school
• Socially handicapped students (2016 National Survey of Competences)	• Elite school (Top 10 in national ranking in 2017)

Group 9/b and the elite school the same test of the level of the elite class.

Group 9/a wrote an easier test of their on level of the same topic.



The percentage of the score of study groups 9/a and the experimental study group 9/b. The red columns denote the scores of the experimental group. Group 9/a had one less problem in the test. Their test was simpler, adjusted to the level of the vocational school.



The percentage of the score of study groups of the elite high school and the experimental study group 9/b. The middle columns denote the scores of the experimental group. The three groups wrote the same test of the level of the class. The pupils of the experimental group and of the elite high school achieved the same result.





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Eötvös Loránd University,
Department of Algebra and Number Theory,
SZEIBERT Janka,
MUZNAY Anna,



Faculty of Natural Science,
1117 Budapest, Pázmány Péter sétány 1/C
SZABÓ Csaba,
ZÁMBÓ Csilla



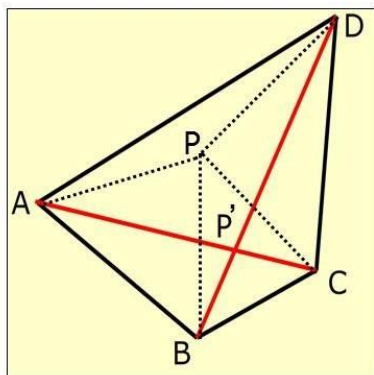
e-mail: szeibert.janka@gmail.com

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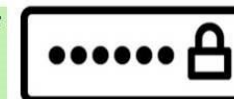
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Poster Section



Fogadás



Fogadás



Néhány darab a mozaikból - közelebbről



- Mogens Niss: The very multi-faceted nature of mathematics education research (PL)
 - Cikkírás fontossága
 - Kialakult stílus
- Markku Hanula: From anxiety to engagement
 - Egyik első kutató
 - Elmúlt években Mo-n is erősen kutatott téma
- Plenary Panel: ...first – high performance or positive affective variables...



Néhány darab a mozaikból - közelebbről



- „Látókör-tágítás”
 - Esztétika a matematikában
 - Kreativitás (vs. Képzelőerő) mérhetősége
 - Tanulók kommunikációjának jellegzetességei csoportmunka során
 - Tanári hiedelemrendszerek szerepe



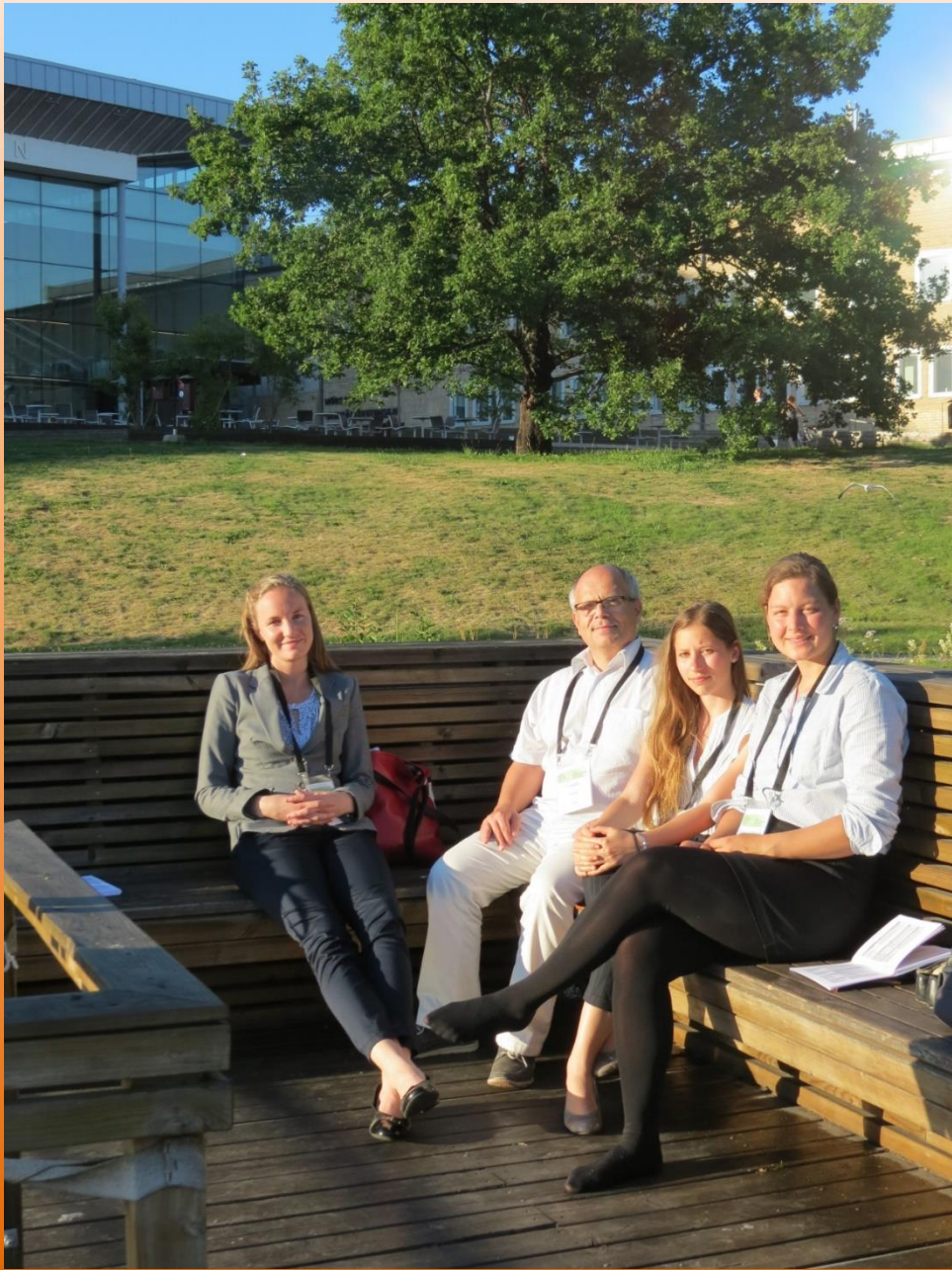
Néhány darab a mozaikból - közelebbről



- Modellezési feladatok
 - Előzetes tudás szerepe
- Tanár(szakos) és/vagy kutató
 - Strohmaier, Anselm R.: Mathematics in disguise: Effects of external context of mathematical word problems
 - Designing for guided reinvention of mathematical concepts

Research Reports No 6.

RR # Room	Author	Title
RR 6:01 N410	Mutara, Lydia; <u>Makonye, Judah</u> <u>Paul</u>	Students' pathways for solving probability problems
RR 6:02 N420	<u>Sievert, Henning</u> ; Van Den Ham, Ann-Kathrin; Niedermeyer, Inga; Heinze, Aiso	Textbook effects on the development of adaptive expertise
RR 6:03 N430	Buforn, Ángela; <u>Fernández,</u> <u>Ceneida</u> ; Llinares, Salvador	Decision-making in noticing students' proportional reasoning
RR 6:04 N440	<u>Fritzlar, Torsten</u> ; Karpinski-Siebold, Nadja	Solving arithmetic-algebraic word problems by 10- to 12-year-old students
RR 6:05 N450	<u>Lisarelli, Giulia</u>	How dragging mediates discourse about functions
RR 6:06 N460	Di Martino, Pietro; <u>Gregorio,</u> <u>Francesca</u>	The first-time phenomenon: Successful student mathematical crisis in secondary-tertiary transition
RR 6:07 N300	<u>Dyrvold, Anneli</u>	Conceptualising translations between representations







Te gusta ▾ Siguiendo ▾ Compartir ...



PME 42

29 de junio · 🌐

Do you like to take a morning run? But you don't know where to run in Umeå? Don't worry! There will be guided running tours at different speed and different distances.

Time and place to meet will be announced at the PME42 Facebook page and on the announcement board at the conference venue.

You can also contact Frithjof at frithjof.theens@umu.se or



Frithjof Theens y 27 personas más

7 comentarios 2 veces compartido

Me gusta

Comentar

Compartir



Más antiguos ▾



Anne-Sophie Supply Jo Van Hoof die loopschoenen gingen mee he?

Me gusta · Responder · Ver traducción · 18 s



3

↪ 12 respuestas



Frithjof Theens The first morning run will be on Wednesday, distance about 5 km, meeting at 7 AM.

Me gusta · Responder · 18 s



3



